

(20 points) Identify the following curve after one clue for 20 points, after two clues for 10 points.

1. Its equation in rectangular coordinates is y equals a over two times the quantity e to the $(x$ over $a)$ plus e to the $(\text{minus } x$ over $a)$.
2. It is the plane curve in which a uniform flexible cables hangs when suspended from two points.

Answer: catenary

(20 points) Pencil and paper ready. Your basic calculus skills will come in handy on this bonus. For 20 points, what is the area located between the y -axis, the x -axis, the line x equals two, and the curve y equals x to the fourth.

Answer: $32/5$, thirty two fifths or 6.4

(20 points) It is an epicycloid of one loop and a special case of the limaçon (limason) and is a plane curve in which the locus of a fixed point on a given circle rolls on an equal but fixed circle. For 20 points, what is this curve whose equation is given in polar coordinates by r equals a minus a cosine θ .

Answer: cardioid

Answer the following questions about numbers for the stated number of points.

1. 5 points. What is the least common multiple of 20 and 24?

Answer: 120

2. 10 points all or nothing. Give the three distinct prime factors of 180.

Answer: 2, 3, 5

3. 5 points: What is the mean of 2,3,4,7, and 9

Answer: 5